2019

# AP<sup>°</sup> Physics C: Electricity and Magnetism

Sample Student Responses and Scoring Commentary Set 1

# Inside:

Free Response Question 1

- **☑** Scoring Guideline
- ☑ Student Samples
- ☑ Scoring Commentary

© 2019 The College Board. College Board, Advanced Placement, AP, AP Central, and the acorn logo are registered trademarks of the College Board. Visit the College Board on the web: collegeboard.org. AP Central is the official online home for the AP Program: apcentral.collegeboard.org.

# AP<sup>®</sup> PHYSICS 2019 SCORING GUIDELINES

## **General Notes About 2019 AP Physics Scoring Guidelines**

- 1. The solutions contain the most common method of solving the free-response questions and the allocation of points for this solution. Some also contain a common alternate solution. Other methods of solution also receive appropriate credit for correct work.
- The requirements that have been established for the paragraph-length response in Physics 1 and Physics 2 can be found on AP Central at <u>https://secure-media.collegeboard.org/digitalServices/pdf/ap/paragraph-length-response.pdf</u>.
- 3. Generally, double penalty for errors is avoided. For example, if an incorrect answer to part (a) is correctly substituted into an otherwise correct solution to part (b), full credit will usually be awarded. One exception to this may be cases when the numerical answer to a later part should be easily recognized as wrong, e.g., a speed faster than the speed of light in vacuum.
- 4. Implicit statements of concepts normally receive credit. For example, if use of the equation expressing a particular concept is worth 1 point, and a student's solution embeds the application of that equation to the problem in other work, the point is still awarded. However, when students are asked to derive an expression, it is normally expected that they will begin by writing one or more fundamental equations, such as those given on the exam equation sheet. For a description of the use of such terms as "derive" and "calculate" on the exams, and what is expected for each, see "The Free-Response Sections Student Presentation" in the *AP Physics; Physics C: Mechanics, Physics C: Electricity and Magnetism Course Description* or "Terms Defined" in the *AP Physics 1: Algebra-Based Course and Exam Description* and the *AP Physics 2: Algebra-Based Course and Exam Description*.
- 5. The scoring guidelines typically show numerical results using the value  $g = 9.8 \text{ m/s}^2$ , but the use of  $10 \text{ m/s}^2$  is of course also acceptable. Solutions usually show numerical answers using both values when they are significantly different.
- 6. Strict rules regarding significant digits are usually not applied to numerical answers. However, in some cases answers containing too many digits may be penalized. In general, two to four significant digits are acceptable. Numerical answers that differ from the published answer due to differences in rounding throughout the question typically receive full credit. Exceptions to these guidelines usually occur when rounding makes a difference in obtaining a reasonable answer. For example, suppose a solution requires subtracting two numbers that should have five significant figures and that differ starting with the fourth digit (e.g., 20.295 and 20.278). Rounding to three digits will lose the accuracy required to determine the difference in the numbers, and some credit may be lost.

## **Question 1**



Note: Figure not drawn to scale.

A very long, thin, nonconducting cylinder of length *L* is centered on the *y*-axis, as shown above. The cylinder has a uniform linear charge density  $+\lambda$ . Point P is located on the *y*-axis at y = c, where L >> c.

(a)

i.

**15 points** 

LO CNV-3.B.a, SP 7.A 1 point

On the figure shown below, draw an arrow to indicate the direction of the electric field at point P due to the long cylinder. The arrow should start on and point away from the dot.



For drawing a	n arrow at point P th	hat points upv	vard
---------------	-----------------------	----------------	------

ii. LO CNV-2.F, SP 7.C 1 point

Describe the shape and location of a Gaussian surface that can be used to determine the electric field at point P due to the long cylinder.

1 point

For describing a Gaussian surface that could be used to determine the electric field at		1 point
point P		
Example: Drawing a cylinder that is coaxial with the thin cylinder		
and whose surface contains point $P$ can be used to determine the electric field at		
point P.		
Note: Credit is earned if the student draws the correct surface on the figure.		

## **Question 1 (continued)**

#### (a) continued

LO CNV-2.C, SP 5.A, 5.E iii.

3 points

Use your Gaussian surface to derive an expression for the magnitude of the electric field at point P. Express your answer in terms of  $\lambda$ , *c*, *L*, and physical constants, as appropriate.

For using Gauss's law to determine the electric field at point P	1 point
$\frac{q_{enc}}{\varepsilon_0} = \int E \cdot dA \therefore \frac{Q}{\varepsilon_0} = EA$	
For correctly substituting for the charge into the equation above	1 point
For correctly substituting for the area or into the equation above	1 point
$\frac{\lambda L}{\varepsilon_0} = E(2\pi cL) \therefore E = \frac{\lambda}{2\pi\varepsilon_0 c} = \frac{2k\lambda}{c}$	

#### LO ACT-1.D, SP 3.C (b)

2 points

A proton is released from rest at point P. On the axes below, sketch the velocity v as a function of position y and the acceleration a as a function of position y for the proton.



For a concave down graph for <i>v</i> as a function of position <i>x</i> that does not start at the		1 point
origin		
For a concave up graph for <i>a</i> as a function of position <i>x</i> that has an asymptote at the		1 point
horizontal axis		

## **Question 1 (continued)**

The original cylinder is now replaced with a much shorter thin, nonconducting cylinder with the same uniform linear charge density  $+\lambda$ , as shown in the figure below. The length of the cylinder to the right of the *y*-axis is *a*, and the length of the cylinder to the left of the *y*-axis is *b*, where a < b.



(c) LO CNV-3.B.a, SP 7.A 2 points

On the figure shown below, draw an arrow to indicate the direction of the electric field at point P due to the shorter cylinder. The arrow should start on and point away from the dot.



For drawing an arrow at point P that points to the right	1 point
For drawing an arrow at point P that points up and to the right	1 point

(d)

i. and ii. LO CNV-2.F, SP 7.A 1 point

Is there a single Gaussian surface that can be used with Gauss's law to derive an expression for the electric field at point P?

\_\_\_\_Yes \_\_\_\_No

If your answer to part (d)(i) is yes, explain how you can use Gauss's law to derive an expression for the field at point P. If your answer to part (d)(i) is no, explain why Gauss's law cannot be applied to derive an expression for the electric field in this case.

For selecting "No" with a valid explanation		1 point
Claim: Select "No."		
Evidence: The length of the cylinder is not much greater than the distance from the		
cylinder to point P and the charge distribution is asymmetric.		
Reasoning: Therefore, cannot use the approximation of the constant magnitude of		
electric field over a cylindrical surface.		

## **Question 1 (continued)**



Note: This figure is shown again for reference.

A student in class argues that using the integral shown below might be a useful approach for determining the electric field at point P.

$$E = \int \frac{1}{4\pi\varepsilon_0} \frac{1}{r^2} \, dq$$

The student uses this approach and writes the following two integrals for the magnitude of the horizontal and vertical components of the electric field at point P.

Horizontal component: 
$$|E_x| = \frac{\lambda}{4\pi\varepsilon_0} \int_{-b}^{a} \frac{x}{(c^2 + x^2)^{3/2}} dx$$
  
Vertical component:  $|E_y| = \frac{\lambda}{4\pi\varepsilon_0} \int_{-b}^{a} \frac{y}{(c^2 + x^2)} dy$ 

(e)

i. LO CNV-3.A, SP 7.A 1 point

One of the two expressions above is not correct. Which expression is not correct?

\_\_\_\_ Horizontal component \_\_\_\_ Vertical component

For correctly selecting "Vertical component"

© 2019 The College Board. Visit the College Board on the web: collegeboard.org. 1 point

## **Question 1 (continued)**

(e) continued

ii. LO CNV-3.A, SP 7.D 4 points

Identify two mistakes in the incorrect expression, and explain how to correct the mistakes.

For indicating the integral is not along the length of the cylinder	
For an appropriate correction	
Claim: Change $dy$ to $dx$ .	
Evidence: The integral is not along the cylinder.	
Reasoning: This change will make the integral valid.	
For indicating the power on the denominator term for the vertical component is incorrect	
For an appropriate correction	
Claim: The power on the term in the denominator should be $3/2$ .	
Evidence: The units of the integrand are not valid. Reasoning: This change will make the integrand valid.	

#### **Learning Objectives**

**ACT-1.D:** Determine the motion of a charged object of specified charge and mass under the influence of an electrostatic force.

**CNV-2.C:** State and use Gauss's law in integral form to derive unknown electric fields for planar, spherical, or cylindrically symmetrical charge distributions.

**CNV-2.F:** Describe the general features of an unknown charge distribution, given other features of the system. **CNV-3.A:** Derive expressions for the electric field of specified charge distributions using integration and the principle of superposition. Examples of such charge distributions include a uniformly charged wire, a thin ring of charge (along the axis of the ring), and a semicircular or part of a semicircular arc.

**CNV-3.B.a:** Identify and qualitatively describe situations in which the direction and magnitude of the electric field can be deduced from symmetry considerations and understanding the general behavior of certain charge distributions.

#### **Science Practices**

**3.C:** Sketch a graph that shows a functional relationship between two quantities.

**5.A:** Select an appropriate law, definition, or mathematical relationship or model to describe a physical situation. **5.E:** Derive a symbolic expression from known quantities by selecting and following a logical algebraic pathway.

**7.A:** Make a scientific claim.

7.C: Support a claim with evidence from physical representations.

7.D: Provide reasoning to justify a claim using physical principles or laws.

## E Q1 A p1 PHYSICS C: ELECTRICITY AND MAGNETISM SECTION II Time—45 minutes 3 Questions

**Directions:** Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in this booklet in the spaces provided after each part.



Note: Figure not drawn to scale.

1. A very long, thin, nonconducting cylinder of length L is centered on the y-axis, as shown above. The cylinder has a uniform linear charge density  $+\lambda$ . Point P is located on the y-axis at y = c, where L >> c.

(a)

- i. On the figure shown below, draw an arrow to indicate the direction of the electric field at point P due to the long cylinder. The arrow should start on and point away from the dot.
- ii. Describe the shape and location of a Gaussian surface that can be used to determine the electric field at point P due to the long cylinder.

iii. Use your Gaussian surface to derive an expression for the magnitude of the electric field at point P. Express your answer in terms of  $\lambda$ , c, L, and physical constants, as appropriate.

$$\begin{aligned} \int \vec{E} \cdot d\vec{s} &= \frac{q_{enc}}{\epsilon_0} \\ \vec{E} \cdot d\vec{s} &= \frac{\lambda}{2\alpha r k_0} \\ \vec{E} \cdot (c) &= \frac{\lambda}{2\kappa c k_0} \end{aligned}$$

Unauthorized copying or reuse of any part of this page is illegal.

GO ON TO THE NEXT PAGE.

© 2019 The College Board. Visit the College Board on the web: collegeboard.org.

-6-



# E Q1 A p2

(b) A proton is released from rest at point P. On the axes below, sketch the velocity v as a function of position y and the acceleration a as a function of position y for the proton.



The original cylinder is now replaced with a much shorter thin, nonconducting cylinder with the same uniform linear charge density  $+\lambda$ , as shown in the figure below. The length of the cylinder to the right of the y-axis is a, and the length of the cylinder to the left of the y-axis is b, where a < b.



(c) On the figure shown below, draw an arrow to indicate the direction of the electric field at point P due to the shorter cylinder. The arrow should start on and point away from the dot.



Question 1 continues on the next page.

Unauthorized copying or reuse of any part of this page is illegal.

#### GO ON TO THE NEXT PAGE.

i. Is there a single Gaussian surface that can be used with Gauss's law to derive an expression for the electric field at point P?

\_Yes <u>√</u>No

ii. If your answer to part (d)(i) is yes, explain how you can use Gauss's law to derive an expression for the field at point P. If your answer to part (d)(i) is no, explain why Gauss's law cannot be applied to derive an expression for the electric field in this case.

because a and b are not with prester than 
$$C$$
, the Held he  
reclarger identative an unitrophical components of the Held he  
from the cylinder connet be upported. Therefore, a shiple consistion  
surface connet be used and y bourse's her connet be upplied,  
$$\frac{P}{y=c} + \lambda = \frac{-b - b - a - b}{2}$$



A student in class argues that using the integral shown below might be a useful approach for determining the electric field at point P.

$$E = \int \frac{1}{4\pi\varepsilon_0} \frac{1}{r^2} \, dq$$

The student uses this approach and writes the following two integrals for the magnitude of the horizontal and vertical components of the electric field at point P.

Horizontal component:

$$|E_x| = \frac{\lambda}{4\pi\varepsilon_0} \int_{-b}^{a} \frac{x}{\left(c^2 + x^2\right)^{3/2}} dx$$

Vertical component:

$$\left|E_{y}\right| = \frac{\lambda}{4\pi\varepsilon_{0}} \int_{-b}^{a} \frac{y}{\left(c^{2} + x^{2}\right)} \, dy$$

(e)

i. One of the two expressions above is not correct. Which expression is not correct?

\_\_\_\_\_ Horizontal component \_\_\_\_\_ Vertical component

ii. Identify two mistakes in the incorrect expression, and explain how to correct the mistakes.

-8-

(d)

## E Q1 B p1 PHYSICS C: ELECTRICITY AND MAGNETISM SECTION II Time-45 minutes 3 Questions

**Directions:** Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in this booklet in the spaces provided after each part.



Note: Figure not drawn to scale.

1. A very long, thin, nonconducting cylinder of length L is centered on the y-axis, as shown above. The cylinder has a uniform linear charge density  $+\lambda$ . Point P is located on the y-axis at y = c, where L >> c.

(a)

i. On the figure shown below, draw an arrow to indicate the direction of the electric field at point P due to the long cylinder. The arrow should start on and point away from the dot.



- ii. Describe the shape and location of a Gaussian surface that can be used to determine the electric field at point P due to the long cylinder.
  - A langard Cylinder I will have unterly that wrops around the p long this cylinder with the side soing through p
- iii. Use your Gaussian surface to derive an expression for the magnitude of the electric field at point P. Express your answer in terms of  $\lambda$ , c, L, and physical constants, as appropriate.

Unauthorized copying or reuse of any part of this page is illegal. (b) A proton is released from rest at point P. On the axes below, sketch the velocity v as a function of position y and the acceleration a as a function of position y for the proton.  $F = v \frac{2}{r^2}$ 

The original cylinder is now replaced with a much shorter thin, nonconducting cylinder with the same uniform linear charge density  $+\lambda$ , as shown in the figure below. The length of the cylinder to the right of the y-axis is a, and the length of the cylinder to the left of the y-axis is b, where a < b.



(c) On the figure shown below, draw an arrow to indicate the direction of the electric field at point P due to the shorter cylinder. The arrow should start on and point away from the dot.



Question 1 continues on the next page.

Unauthorized copying or reuse of any part of this page is illegal.

GO ON TO THE NEXT PAGE.

-7-

i. Is there a single Gaussian surface that can be used with Gauss's law to derive an expression for the electric field at point P?

\_Yes \_X\_No

ii. If your answer to part (d)(i) is yes, explain how you can use Gauss's law to derive an expression for the field at point P. If your answer to part (d)(i) is no, explain why Gauss's law cannot be applied to derive an expression for the electric field in this case.





A student in class argues that using the integral shown below might be a useful approach for determining the electric field at point P.

$$E = \int \frac{1}{4\pi\varepsilon_0} \frac{1}{r^2} \, dq$$

The student uses this approach and writes the following two integrals for the magnitude of the horizontal and vertical components of the electric field at point P.

Horizontal component:

$$\left|E_{x}\right| = \frac{\lambda}{4\pi\varepsilon_{0}} \int_{-b}^{a} \frac{x}{\left(c^{2} + x^{2}\right)^{3/2}} dx$$

Vertical component:

$$\left|E_{y}\right| = \frac{\lambda}{4\pi\varepsilon_{0}}\int_{-b}^{a}\frac{y}{\left(c^{2}+x^{2}\right)}dy$$

(e)

Unauthoriz any part of i. One of the two expressions above is not correct. Which expression is not correct?

\_\_\_\_Horizontal component \_\_\_\_\_Vertical component

ii. Identify two mistakes in the incorrect expression, and explain how to correct the mistakes.

(d)

### E Q1 C p1 PHYSICS C: ELECTRICITY AND MAGNETISM SECTION II Time-45 minutes 3 Questions

**Directions:** Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in this booklet in the spaces provided after each part.



Note: Figure not drawn to scale.

1. A very long, thin, nonconducting cylinder of length L is centered on the y-axis, as shown above. The cylinder has a uniform linear charge density  $+\lambda$ . Point P is located on the y-axis at y = c, where L >> c.

(a)

i. On the figure shown below, draw an arrow to indicate the direction of the electric field at point P-due to the long cylinder. The arrow should start on and point away from the dot.



ii. Describe the shape and location of a Gaussian surface that can be used to determine the electric field at point P due to the long cylinder.



iii. Use your Gaussian surface to derive an expression for the magnitude of the electric field at point P. Express your answer in terms of  $\lambda$ , c, L, and physical constants, as appropriate.

$$EA = \frac{2enc}{\varepsilon_o}$$

$$E(\pi c^2 L) = \frac{2enc}{\varepsilon_o}$$

$$E = \frac{\lambda L}{\pi c^2 L} = \frac{\lambda}{\pi c^2}$$

$$\frac{1}{\sigma^2 L} = \frac{\lambda}{\sigma^2}$$
Go on to the next page.

Unauthorized copying or reuse of any part of this page is illegal.

# (b) A proton is released from rest at point P. On the axes below, sketch the velocity v as a function of position y and the acceleration a as a function of position y for the proton.



The original cylinder is now replaced with a much shorter thin, nonconducting cylinder with the same uniform linear charge density  $+\lambda$ , as shown in the figure below. The length of the cylinder to the right of the y-axis is a, and the length of the cylinder to the left of the y-axis is b, where a < b.



(c) On the figure shown below, draw an arrow to indicate the direction of the electric field at point P due to the shorter cylinder. The arrow should start on and point away from the dot.



Question 1 continues on the next page.

Unauthorized copying or reuse of any part of this page is illegal.

#### GO ON TO THE NEXT PAGE.

# E Q1 C p3

i. Is there a single Gaussian surface that can be used with Gauss's law to derive an expression for the electric field at point P?

ii. If your answer to part (d)(i) is yes, explain how you can use Gauss's law to derive an expression for the field at point P. If your answer to part (d)(i) is no, explain why Gauss's law cannot be applied to derive an expression for the electric field in this case.





A student in class argues that using the integral shown below might be a useful approach for determining the electric field at point P.

$$E = \int \frac{1}{4\pi\varepsilon_0} \frac{1}{r^2} \, dq$$

The student uses this approach and writes the following two integrals for the magnitude of the horizontal and vertical components of the electric field at point P.

Horizontal component:

Vertical component:

$$\left|E_{y}\right| = \frac{\lambda}{4\pi\varepsilon_{0}} \int_{-b}^{a} \frac{y}{\left(c^{2} + x^{2}\right)} dy$$

 $|E_x| = \frac{\lambda}{4\pi\varepsilon_0} \int_{-b}^{a} \frac{x}{(c^2 + x^2)^{3/2}} dx \frac{\gamma}{4\pi\varepsilon_0} \int_{-c^2 + x^2}^{x} dx$ 

(e)

i. One of the two expressions above is not correct. Which expression is not correct?

Horizontal component \_\_\_\_\_ Vertical component

ii. Identify two mistakes in the incorrect expression, and explain how to correct the mistakes.

Unauthorized copying or reuse of any part of this page is illegal.

#### GO ON TO THE NEXT PAGE.

-8-

© 2019 The College Board. Visit the College Board on the web: collegeboard.org.

(d)

# AP<sup>®</sup> PHYSICS C: ELECTRICITY AND MAGNETISM 2019 SCORING COMMENTARY

## Question 1

Note: Student samples are quoted verbatim and may contain spelling and grammatical errors.

#### Overview

The responses to this question were expected to demonstrate the following:

- An understanding of the properties of the electric field due to a charge distribution
- The ability to use Gauss's law
- The ability to identify an appropriate Gaussian surface
- The ability to graphically describe the motion of a charged particle in an electric field
- An understanding of when Gauss's law is an appropriate approach to solve a problem
- The ability to separate a vector into components
- The ability to carry out integration along a line

#### Sample: E Q1 A Score: 15

All parts of this response earned full credit. Part (a)(i) has an arrow pointing upward, so 1 point was earned. Part (a)(ii) describes an appropriate Gaussian surface, so 1 point was earned. Part (a)(iii) correctly substitutes the area and charge into Gauss's law, so 3 points were earned. Part (b) has a concave down curve for the velocity-position graph that does not start at the origin, and a concave down curve for the acceleration graph with a horizontal axis asymptote, so 2 points were earned. Part (c) has an arrow pointing up and to the right, so 2 points were earned. Part (d) has a correct selection and valid explanation, so 1 point was earned. Part (e) has a correct selection and correctly identifies two mistakes with appropriate corrections, so 5 points were earned.

#### Sample: E Q1 B Score: 10

Parts (a)(i), (a)(ii), (c), and (d) earned full credit, 1 point, 1 point, 2 points, and 1 point, respectively. Part (a)(iii) uses Gauss's law but incorrectly substitutes for the charge and does not substitute for the radius, so 1 point was earned. Part (b) has a concave down curve for the acceleration graph with a horizontal axis asymptote but incorrectly starts the velocity graph at the origin, so 1 point was earned. Part (e) has a correct selection but only correctly identifies one mistake with appropriate correction, so 3 points were earned.

#### Sample: E Q1 C Score: 5

Parts (a)(i) and (c) earned full credit, 1 point and 2 points, respectively. Part (a)(ii) describes an appropriate Gaussian surface but does not indicate that it is coaxial with the original cylinder, so no points were earned. Part (a)(iii) uses Gauss's law and substitutes correctly for the charge but uses an incorrect area, so 2 points were earned. Part (b) has two incorrect graphs, so no points were earned. Part (d) has an incomplete statement, so no points were earned. Part (e) has an incorrect selection and does not correctly identify any mistakes, so no points were earned.